

## Joule Heating Effect in Presence of Thermal Radiation on MHD Convective Flow Past Over A Vertical Surface in A Porous Medium

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**Abstract:** This paper presents the effects of Joule heating and viscous dissipation on magneto-hydrodynamic convection flow of steady, viscous, incompressible and electrically conducting fluid past a semi infinite vertical plate embedded in a porous medium in presence of thermal radiation with constant heat and mass fluxes. The governing partial differential equations are converted into a set of ordinary differential equations using non dimensional quantities. Perturbation method has been applied to solve the system of partial differential equations. The expressions for skin-friction, rate of heat transfer, and rate of mass transfer are also derived. The effects of various physical parameters, encountered in the problem, on the velocity field, temperature field, and concentration field are shown numerically through graphs.

**Keywords:** Chemical reaction, Radiation, MHD, Joule heating, heat and mass fluxes, Perturbation technique.

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### NOMENCLATURE

$C$  : Concentration of species  
 $D$  : Chemical molecular diffusivity  
 $q$  : Constant heat flux  
 $m$  : Constant mass flux  
 $g$  : Acceleration due to gravity  
 $M$  : Magnetic parameter  
 $N_u$  : Nusselt Number  
 $C_p$  : Specific molecular diffusivity  
 $Gm$  : Grashof number for mass transfer  
 $P_r$  : Prandtl number  
 $Sc$  : Schmidt number  
 $T$  : The fluid temperature  
 $T_\infty$  : The fluid temperature at infinity  
 $v_0$  : Scale of suction velocity  
 $B_0$  : Magnetic flux density  
 $Sh$  : Sherwood number  
 $C_\infty$  : Species concentration at infinity  
 $F$  : Radiation Parameter  
 $Gr$  : Grashof number for heat transfer  
 $Gm$  : Grashof number for mass transfer  
 $Kr$  : Chemical reaction parameter  
 $E$  : Eckert Number

### Greek symbols

$\alpha$  : Permeability parameter  
 $\beta_1$  : The volumetric coefficient expansion due to temperature

$\beta_2$  : Coefficient of the volume expansion with species concentration

$\mu$  : Dynamic viscosity

$k_p$  : Permeability of porous medium

$\theta(\eta)$  : Dimensionless temperature

$\nu$  : Kinematic viscosity

$\rho$  : Density of the fluid

$\lambda$  : Thermal conductivity

$\sigma$  : Electrical conductivity

$\tau$  : Skin fraction

$\eta$  : Distance

## I. INTRODUCTION

In industrial and real life problems, there exist flows which are stimulated not only by the differences of temperature but also by differences of concentration. These mass transfer differences affect the rate of heat transfer. The phenomenon of heat and mass transfer frequently exists in many chemical processes industries like food processing and polymer process. Free convection flows are of great interest in many industrial applications such as fiber and granular insulation, geothermal systems etc. Lin & Wu (1995) had investigated Simultaneous effect of heat and mass transfer in laminar free convection boundary-layer flow along a vertical plate. Chamkha (2004) have carried out the unsteady MHD convective heat and mass transfer over a semi-infinite vertical permeable moving plate with heat absorption.

The study of Magneto-hydrodynamics(MHD) with heat and mass transfer in the presence of radiation has attracted many researchers due to diverse applications in different areas of sciences and technologies. Effect of radiation on MHD is of considerable interest because of its wider applications in space technology and other area of technology and sciences. Many researchers studied the effect of radiation on magneto hydrodynamic free convection flows under diverse surface boundary conditions using different techniques of Mathematics. Lot of engineering processes takes place at high temperatures and so the knowledge of radiation and heat transfer is essential for designing various types of industrial equipments. Nuclear power plants, gas turbines and various propulsion devices for aircraft, missiles and satellites are some examples of such processes. Cogley (1968) developed differential approximations for radiative heat transfer in a non-linear equations non-grey gas near equilibrium. The unsteady hydro magnetic free convection flow with radioactive transfer in a rotating fluid was discussed by Bestman and Adjepong (1998). Hossain et al. (1999) had analyzed the effect of radiation on free convection from a porous vertical plate. Combined free convective boundary-layer flow with thermal radiation and mass transfer past a moving vertical porous plate, when the plate moves in its own plane was studied by Makinde (2005). Pathak and Maheshwari [2006] discussed the influence of radiation on an unsteady free convection flow bounded by an oscillating plate with variable wall temperature. Mamun et al.(2008) analyzed the conjugate effect of heat transfer and MHD for a vertical plate in presence of viscous dissipation and heat generation. Mankinde and Aziz (2010) discussed MHD mixed convection from a vertical plate embedded in a porous medium with a convective boundary condition. Rajesh and Verma (2010) introduced radiation effects on MHD flow through a porous medium with variable temperature and mass diffusion. Saxena, and Dubey (2011) investigated MHD free convection heat and mass transfer flow of visco-elastic fluid embedded in a porous medium with variable permeability, radiation effect and heat source in slip flow region. Sudhakar et. al. (2013) analyzed the effect of chemical reaction and radiation on MHD free convective flow through a porous medium bounded by a vertical surface in presence of constant heat and mass fluxes. The velocity slips effects on the heat and mass fluxes of a viscous electrically conducting fluid flow over a stretching sheet in the presence of viscous dissipation, Ohmic dissipation and thermal radiation have discussed by Kayalvizhi et al. (2016).

Chemical reactions can be coded either as heterogeneous or homogeneous processes. They depend on whether they occur at an interface or as a single phase volume reaction. The reaction is heterogeneous if it takes place at an interface level and homogeneous if it takes place in solution. In most of chemical reactions, the reaction rate depends on the concentration of the species. The first ordered chemical reaction in the neighborhood of a horizontal plate has been examined by Chambre and Young (1958). The effects of chemical reaction, thermophoresis and variable viscosity on a study of hydro magnetic flow with heat and mass transfer over a flat plate in the presence of heat generation/absorption was examined by Seddeek (2005). Al-Mudhaf and Chamkha [2005] analyzed the MHD thermosolutal Marangoni convection boundary layer. They have studied the effects of heat generation/absorption, Hartmann number, the chemical reaction parameter and the suction/injection parameter on the flow. The effect of chemical reaction and radiation absorption on free convection flow through porous medium with variable suction in the presence of uniform magnetic field was

investigated by Sudheer Babu and Satyanarayana (2009). The case of unsteady MHD convective heat and mass transfer in a boundary layer slip flow over a vertical permeable with thermal radiation and chemical reaction was examined by Pal et al. (2010). Kishan and Amrutha (2010) analyzed the effects of viscous dissipation on MHD flow with heat and mass transfer over a stretching surface with heat source. Sarada and Shanker (2013) have investigated the effect of chemical reaction on an unsteady magneto hydrodynamic flow over an infinite vertical porous plate with variable suction and heat convective mass transfer, where the plate temperature oscillates with the frequency as that of variable suction velocity. Effect of chemical reaction on MHD flow of continuously moving vertical surface with heat and mass flux through porous medium has been discussed by Girish Kumar (2013). Mangathai et al. (2015) have presented an exact analysis of combined effects of radiation and chemical reaction on the magneto hydrodynamic (MHD) free convection flow of an electrically conducting incompressible viscous fluid over an inclined plate embedded in a porous medium.

The effects of Joule heating is usually characterized by the product of the Eckert number and magnetic parameter. It have a very important rule in geophysical flows and in nuclear. With this understanding, many researchers studied the effects of Joule heating in various geometries. Alim et al [2007] analyzed the effects of suction or injection on boundary layer flow. Palani and Kim (2011) employed implicit finite difference scheme of Crank-Nicolson method to analyze the importance of Joule heating and viscous dissipation effects on MHD flow along inclined plate subject to variable surface temperature.

The present work is concerned with the effect of thermal radiation and joule heating on magneto hydrodynamic convection flow of steady, viscous, incompressible and electrically conducting fluid past a semi infinite vertical plate embedded in a porous medium. Here, we assume that a chemically reactive species is emitted from the surface and diffuses into the fluid. The reaction is assumed to take place entirely in the stream. The governing partial differential equations have been converted into a set of ordinary differential equations using non dimensional quantities. Perturbation technique has been applied to solve the system of partial differential equations. The effects of various governing parameters on the velocity, temperature, concentration, skin friction coefficient, rate of heat transfer and rate of mass transfer will be shown and discussed.

## II. MATHEMATICAL ANALYSIS

Consider two dimension steady flow of a viscous incompressible electrically conducting fluid through a porous medium occupying semi infinite region of space bounded by a vertical infinite surface subjected to a thermal radiation and joule heating. The  $x^*$  axis is chosen along the plate and the  $y^*$  axis is perpendicular to it. The uniform magnetic field of strength  $B_0$  in the presence of radiation and joule heating is imposed transversely in the direction of  $y^*$  axis. The induced magnetic field is neglected under the assumption that the magnetic Reynolds number is small. The properties of fluid are assumed to be constant except for the density. A chemically reactive species is emitted from the vertical surface into a hydrodynamic flow field. It diffuses into the fluid, where it undergoes a homogeneous chemical reaction. The reaction is assumed to take place entirely in the stream. The governing equations for the study are based on the conservation of mass, linear momentum and energy.

Taking into consideration the assumptions made above, equations in Cartesian frame of reference are given by

Continuity equation

$$\frac{\partial v^*}{\partial y^*} = 0$$

(1)

Momentum equation

$$v^* \frac{\partial u^*}{\partial y^*} = \nu \frac{\partial^2 u^*}{\partial y^{*2}} + g\beta_1(T^* - T_\infty) + g\beta_2(C^* - C_\infty) - \frac{\nu u^*}{k_p} - \frac{\sigma B_0^2 u^*}{\rho}$$

(2)

Energy equation

$$v^* \frac{\partial T^*}{\partial y^*} = \frac{\lambda}{\rho C_p} \frac{\partial^2 T^*}{\partial y^{*2}} + \frac{\nu}{C_p} \left( \frac{\partial u^*}{\partial y^*} \right)^2 - \frac{1}{\rho C_p} \frac{\partial q_r}{\partial y^*} - \frac{\sigma B_0^2}{\rho C_p} u^{*2}$$

(3)

Species equation

$$v^* \frac{\partial C^*}{\partial y^*} = D \frac{\partial^2 C^*}{\partial y^{*2}} - k_c C^* \quad (4)$$

Where  $u^*$  and  $v^*$  are the components of the dimensional velocities along  $x^*$  and  $y^*$  directions respectively.

Let the level of species concentration is very low. Therefore the heat generated due to the chemical reaction is neglected.

From equation (1),

$$v^* = \text{constant} = -v_0 \quad (5)$$

Where  $v_0 > 0$  corresponding to steady suction velocity normal at the surface and  $v$  is the steady normal velocity of suction on the surface.

Cogley et al. [1968] have shown that in the optically thin limit for a non-gray gas near equilibrium, the radiative heat flux is represented by the following form:

$$\frac{\partial q_r}{\partial y^*} = 4(T^* - T_\infty) I^* \quad (6)$$

Where  $I^* = \int K_\lambda \frac{\partial e_\lambda}{\partial T^*} d\lambda$ ,  $K_\lambda$  the absorption coefficient at the plate and  $e_\lambda$  be the plank's function.

The relevant boundary conditions are

$$\left. \begin{aligned} u^* = 0, T^* = T_\infty, C^* = C_\infty \text{ for any value of } y^*, t \leq 0 \\ u^* = 0, \frac{\partial T^*}{\partial y^*} = -\frac{q}{\lambda}, \frac{\partial C^*}{\partial y^*} = -\frac{m}{D}, y^*, t > 0 \\ u^* \rightarrow 0, T^* \rightarrow T_\infty, C^* \rightarrow C_\infty, y^* \rightarrow \infty, t > 0 \end{aligned} \right\} \quad (7)$$

Using equation (5), equations (2), (3) and (4) reduces to

$$-v^* \frac{\partial u^*}{\partial y^*} = v \frac{\partial^2 u^*}{\partial y^{*2}} + g\beta_1(T^* - T_\infty) + g\beta_2(C^* - C_\infty) - \frac{vu^*}{k_p} - \frac{\sigma B_0^2 u^*}{\rho} \quad (8)$$

$$-v^* \frac{\partial T^*}{\partial y^*} = \frac{\lambda}{\rho C_p} \frac{\partial^2 T^*}{\partial y^{*2}} + \frac{v}{C_p} \left( \frac{\partial u^*}{\partial y^*} \right)^2 - \frac{1}{\rho C_p} \frac{\partial q_r}{\partial y^*} - \frac{\sigma B_0^2}{\rho C_p} u^{*2} \quad (9)$$

$$-v^* \frac{\partial C^*}{\partial y^*} = D \frac{\partial^2 C^*}{\partial y^{*2}} - k_c C^* \quad (10)$$

Now, we introduce the dimensionless variables as follows

$$\left. \begin{aligned} f(\eta) = \frac{u^*}{v_0}, \eta = \frac{v_0 y^*}{\nu}, \text{Pr} = \frac{\nu \rho C_p}{\lambda}, F = \frac{4\nu^2 I^*}{\lambda v_0^2}, \alpha = \frac{v_0^2 k_p}{\nu^2}, C = \frac{(C^* - C_\infty)D}{m}, \\ G_r = \frac{g\beta_1 q \nu}{\lambda v_0^3}, S_c = \frac{\nu}{D}, \theta = \frac{(T^* - T_\infty)\lambda}{\nu q}, Kr = \frac{k_c \nu}{v_0^2}, M = \frac{\sigma \nu B_0^2}{\rho v_0^2}, E = \frac{\lambda v_0^2}{q C_p}, Gm = \frac{g\beta_2 m \nu}{D v_0^3} \end{aligned} \right\} \quad (11)$$

Using (11), the governing equations (8), (9) and (10) reduce to the following form:

$$f'' + f' - \left( \frac{1}{\alpha} + M \right) f = -Gr\theta - GmC \quad (12)$$

$$\theta'' + \text{Pr} \theta' - F\theta = -E \text{Pr} (f')^2 - \text{Pr} EMf'^2 \quad (13)$$

$$C'' + \text{Sc}C' = \text{Sc}K_r C \quad (14)$$

where all primes are w.r.to  $\eta$ .

The boundary conditions (7) in the dimensionless form can be written as

$$\left. \begin{aligned} \eta = 0, f = 0, \theta' = -1, C' = -1 \\ \eta \rightarrow \infty, f \rightarrow 0, \theta \rightarrow 0, C \rightarrow 0 \end{aligned} \right\} \quad (15)$$

### III. SOLUTION OF THE PROBLEM

To obtain the solution of above coupled non linear system of equations (12)-(14) with the boundary conditions (15), we expand  $f, \theta$  and  $C$  in powers of Eckert number  $E$  assuming that it is very small. This is justified in low speed incompressible flow. Hence we can write

$$\left. \begin{aligned} f = f_0 + Ef_1 + o(E^2) \\ \theta = \theta_0 + E\theta_1 + o(E^2) \\ C = C_0 + Ef_1 + o(E^2) \end{aligned} \right\} \quad (16)$$

Substituting equations (16) into equations (12)-(14) and equating like powers of  $E$  and neglecting the coefficient of  $O(E^2)$ , we get the following pairs of equations

$$f_0'' + f_0' - \delta f_0 = -Gr \theta_0 - GmC_0 \quad (17)$$

$$f_1'' + f_1' - \delta f_1 = -Gr \theta_1 - GmC_1 \quad (18)$$

$$\theta_0'' + \text{Pr} \theta_0' = F\theta_0 \quad (19)$$

$$\theta_1'' + \text{Pr} \theta_1' - F\theta_1 = -\text{Pr} f_0'^2 - \text{Pr} Mf_0'^2 \quad (20)$$

$$C_0'' + \text{Sc}C_0' = \text{Sc}K_r C_0 \quad (21)$$

$$C_1'' + \text{Sc}C_1' = \text{Sc}K_r C_1 \quad (22)$$

The corresponding boundary conditions can be written as

$$\left. \begin{aligned} f_0 = 0, f_1 = 0, \theta_0' = -1, \theta_1' = 0, C_0' = -1, C_1' = 0, \text{ at } \eta = 0 \\ f_0 \rightarrow 0, f_1 \rightarrow 0, \theta_0 \rightarrow 0, \theta_1 \rightarrow 0, C_0 \rightarrow 0, C_1 \rightarrow 0, \text{ at } \eta \rightarrow \infty \end{aligned} \right\} \quad (23)$$

The solutions of equations (17)-(22) which satisfy the boundary conditions (23) are given by

$$f_0 = K_3 e^{h_2 \eta} + K_1 e^{e_2 \eta} + K_2 e^{d_2 \eta} \quad (24)$$

$$\begin{aligned} f_1 = & K_{30} e^{h_2 \eta} + K_{17} e^{e_2 \eta} + K_{18} e^{2h_2 \eta} + K_{19} e^{2e_2 \eta} + K_{20} e^{2d_2 \eta} + K_{21} e^{(h_2+e_2)\eta} + K_{22} e^{(d_2+e_2)\eta} \\ & + K_{23} e^{(d_2+h_2)\eta} + K_{24} e^{2h_2 \eta} + K_{25} e^{2e_2 \eta} + K_{26} e^{2d_2 \eta} + K_{27} e^{(e_2+h_2)\eta} + K_{28} e^{(d_2+e_2)\eta} + K_{29} e^{(h_2+d_2)\eta} \end{aligned} \quad (25)$$

$$\theta_0 = -\frac{1}{e_2} e^{e_2 \eta} \quad (26)$$

$$\theta_1 = K_{16} e^{e_2 \eta} + K_4 e^{2h_2 \eta} + K_5 e^{2e_2 \eta} + K_6 e^{2d_2 \eta} + K_7 e^{(h_2+e_2)\eta} + K_8 e^{(d_2+e_2)\eta} + K_9 e^{(d_2+h_2)\eta} + K_{10} e^{2h_2 \eta} + K_{11} e^{2e_2 \eta} + K_{12} e^{2d_2 \eta} + K_{13} e^{(e_2+h_2)\eta} + K_{14} e^{(d_2+e_2)\eta} + K_{15} e^{(d_2+h_2)\eta}$$

(27)

$$C_0 = -\frac{1}{d_2} e^{d_2 \eta}$$

(28)

$$C_1 = 0$$

(29)

Substituting the solutions of equations (24)-(28) in (16), we obtain

$$f(\eta) = K_3 e^{h_2 \eta} + K_1 e^{e_2 \eta} + K_2 e^{d_2 \eta} + E(K_{30} e^{h_2 \eta} + K_{17} e^{e_2 \eta} + K_{18} e^{2h_2 \eta} + K_{19} e^{2e_2 \eta} + K_{20} e^{2d_2 \eta} + K_{21} e^{(h_2+e_2)\eta} + K_{22} e^{(d_2+e_2)\eta} + K_{23} e^{(d_2+h_2)\eta} + K_{24} e^{2h_2 \eta} + K_{25} e^{2e_2 \eta} + K_{26} e^{2d_2 \eta} + K_{27} e^{(e_2+h_2)\eta} + K_{28} e^{(d_2+e_2)\eta} + K_{29} e^{(d_2+h_2)\eta}$$

(30)

$$\theta(\eta) = -\frac{1}{e_2} e^{e_2 \eta} + E(K_{16} e^{e_2 \eta} + K_4 e^{2h_2 \eta} + K_5 e^{2e_2 \eta} + K_6 e^{2d_2 \eta} + K_7 e^{(h_2+e_2)\eta} + K_8 e^{(d_2+e_2)\eta} + K_9 e^{(d_2+h_2)\eta} + K_{10} e^{2h_2 \eta} + K_{11} e^{2e_2 \eta} + K_{12} e^{2d_2 \eta} + K_{13} e^{(e_2+h_2)\eta} + K_{14} e^{(d_2+e_2)\eta} + K_{15} e^{(d_2+h_2)\eta})$$

(31)

$$C(\eta) = -\frac{1}{d_2} e^{d_2 \eta}$$

(32)

The rate of heat transfer in terms of the Nusselt number is given by

$$N_u = -\left(\frac{\partial \theta}{\partial \eta}\right)_{\eta=0} = 1 - E[K_{16} e_2 + 2K_4 h_2 + 2K_5 e_2 + 2K_6 d_2 + (e_2 + h_2)K_7 + (d_2 + e_2)K_8 + (d_2 + h_2)K_9 + 2K_{10} h_2 + 2K_{11} e_2 + 2K_{12} d_2 + (e_2 + h_2)K_{13} + (d_2 + e_2)K_{14} + (d_2 + h_2)K_{15}]$$

(33)

The rate of mass transfer in term of Sherwood number (Sh) is given by

$$Sh = \left(\frac{\partial C}{\partial \eta}\right)_{\eta=0} = -1 + E * (-1) = -(1 + E)$$

(34)

The non dimensional skin friction ( $\tau$ ) at the surface is given by

$$\tau = \left(\frac{\partial f}{\partial \eta}\right)_{\eta=0} = K_3 a_6 + K_1 e_2 + K_2 d_2 + E[K_{30} h_2 + K_{17} e_2 + 2K_{18} h_2 + 2K_{19} e_2 + 2K_{20} d_2 + 2K_{21} a_6 + K_{21} (e_2 + h_2) + K_{22} (d_2 + e_2) + K_{23} (d_2 + h_2) + 2K_{24} h_2 + 2K_{25} e_2 + 2K_{26} d_2 + K_{27} (e_2 + h_2) + K_{28} (e_2 + d_2) + K_{29} (d_2 + h_2)]$$

(35)

#### IV. RESULT AND DISCUSSION

The problem of the influence of radiation and joule heating on magneto hydrodynamic steady convective heat and mass transfer past a semi-infinite vertical porous plate by perturbation technique is dealt. Based on these assumptions, we have carried out numerical computations for the velocity, temperature and concentration for various values of the material parameters like Permeability parameter ( $\alpha$ ), Grashof number for heat transfer (Gr), Grashof number for mass transfer (Gm), Prandtl number (Pr), Magnetic parameter (M), Chemical reaction parameter (Kr), Schmidt number (Sc), Eckert Number (E) etc.

**4.1 VELOCITY PROFILES** The velocity profiles are depicted in figures 1-8. Fig.1 displays the effects of permeability coefficient of a porous medium ( $\alpha$ ) velocity profile. It is observed that velocity decreases with

increase in  $(\alpha)$ . It is interesting to observe that the fluid velocity increases and reaches its maximum over a very short distance from the plate and then decreases gradually to zero for positive value of  $\alpha$ . Fig.2 displays the effects of chemical reaction parameter ( $Kr$ ). It is observed that velocity decreases with increase in  $Kr$ . Fig.3 shows the effect of Schmidt Number ( $Sc$ ) on the velocity profile. An increase in Schmidt Number ( $Sc$ ) results in decrease in the velocity. Fig. 4 shows the effect of  $Gr$  on velocity. Velocity increases with increasing  $Gr$ . Fig.5 shows the effect of Eckert Number ( $E$ ) on the velocity profile. An increase in Eckert Number ( $E$ ) results in decrease in the velocity. Effect of  $Gm$  on velocity has been displayed by Fig. 6. It is seen that velocity increases with increasing  $Gm$ . Effect of Radiation parameter ( $F$ ) on the velocity profile is depicted in Fig.7. It is observed that the velocity increases with increase in radiation parameter. Effect of Prandtl Number ( $Pr$ ) on the velocity profile is depicted in Fig. 8. It is observed that the velocity decreases with increase in Prandtl Number ( $Pr$ ). The skin friction has been depicted in Fig. 17. It is observed that skin friction decreases with increasing  $\alpha$  and  $Gr$ .

**4.2 TEMPERATURE PROFILES** The temperature profiles are depicted in figures 9-13. Fig. 9 shows the effect of permeability parameter ( $\alpha$ ) on temperature. It is observed that temperature is directly proportional to  $(\alpha)$ . In Fig.10, the influence of Eckert Number ( $E$ ) on temperature is shown. It is seen that the temperature increases with increase in Eckert Number ( $E$ ). Effect of chemical reaction parameter ( $Kr$ ) on the temperature is depicted in Fig. 11. It is observed that the temperature decreases with increase in chemical reaction parameter ( $Kr$ ). The Effect of Radiation parameter ( $F$ ) on the temperature is depicted in Fig.12. It is observed that the temperature decreases with increase in Radiation parameter ( $F$ ). Fig.13 displays the effects of Mass Grashof Number ( $Gm$ ). It is observed that temperature increases with increasing  $Gm$ . A variation in the heat transfer rate in terms of the Nusselt number  $N$  is shown in figures 16 and 18. It is observed that  $N$  decreases with increasing  $Gr$  and increases with with increasing  $Kr$ .

**4.3 CONCENTRATION PROFILES** The concentration profiles are depicted in figures 14-15. The effect of Schmidt Number ( $Sc$ ) on the concentration is presented in figure 14. It is noted that the concentration decreases with increase in Schmidt Number ( $Sc$ ). In figure 15, the effect of chemical reaction parameter ( $Kr$ ) on the concentration is presented. It is seen that the concentration decreases with increase in chemical reaction parameter ( $Kr$ ).

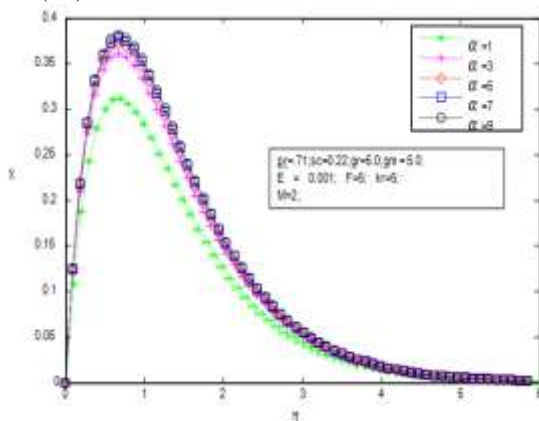


Fig.1 Velocity profile for different value of Permeability parameter ( $\alpha$ )

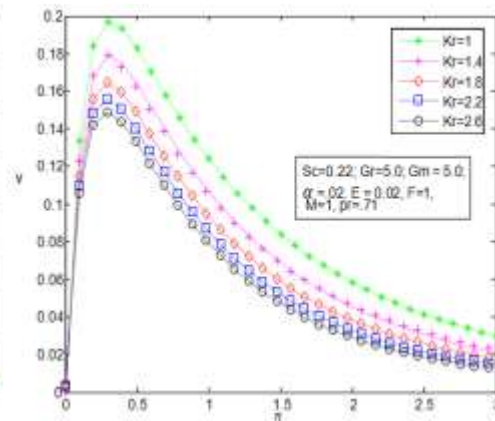


Fig.2 Velocity profile for different value of Chemical Reaction parameter ( $Kr$ )

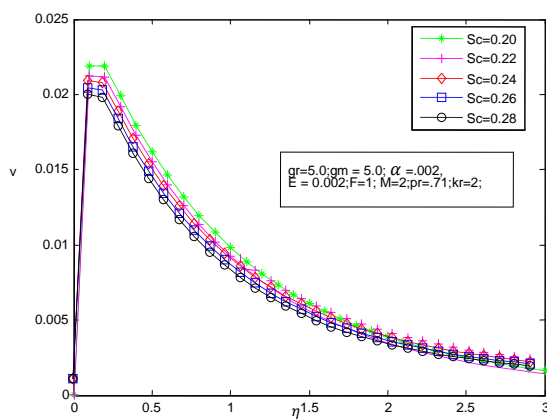


Fig.3 Velocity profile for different value of

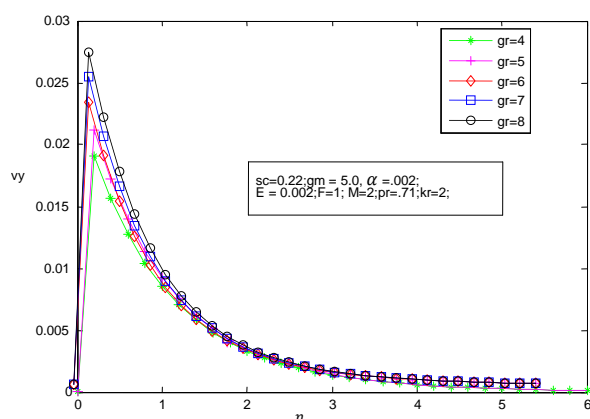


Fig.4 Velocity profile for different value of

Schmidt Number (Sc)

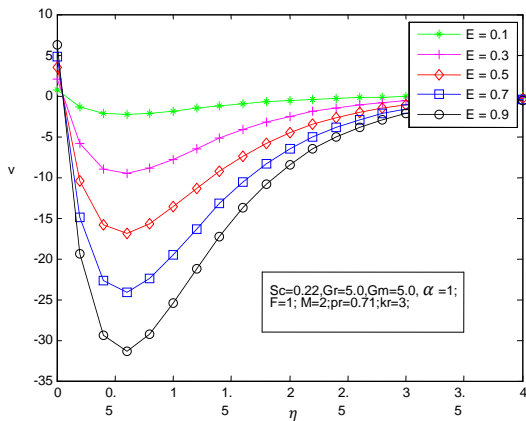


Fig.5 Velocity profile for different value of Grashof number for mass transfer (Gm)

Grashof number for heat transfer(Gr)

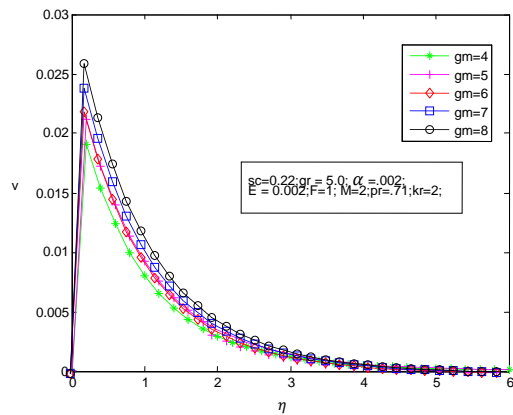


Fig.6 Velocity profile for different value of Eckert Number (E)

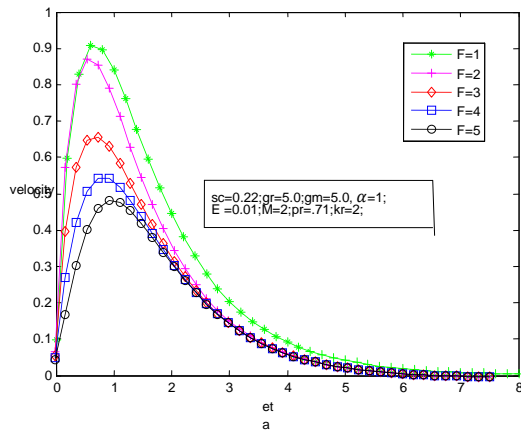


Fig.7 Velocity profile for different value of Radiation Parameter (F)

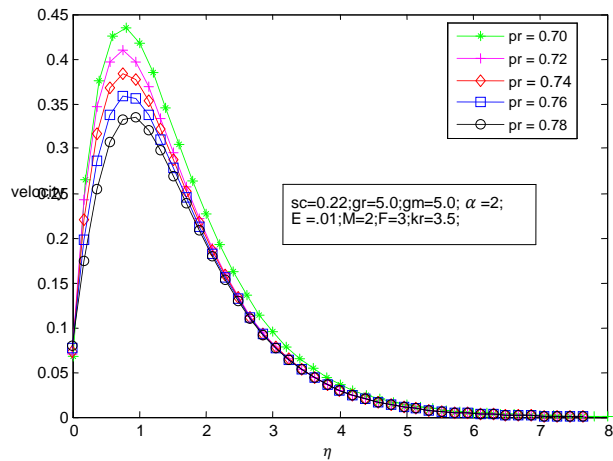


Fig.8 Velocity profile for different value of Prandtl Number (Pr).

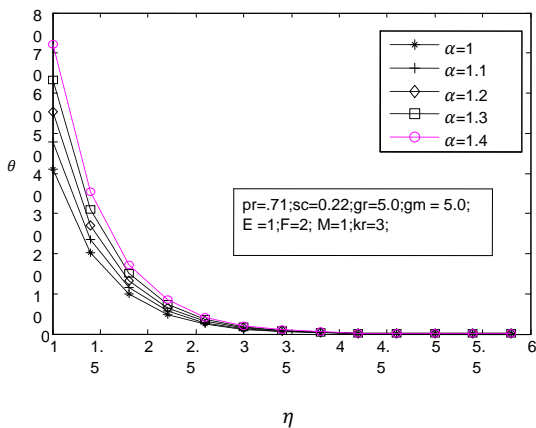


Fig.9 Temperature profile for different value of permeability parameter ( $\alpha$ )

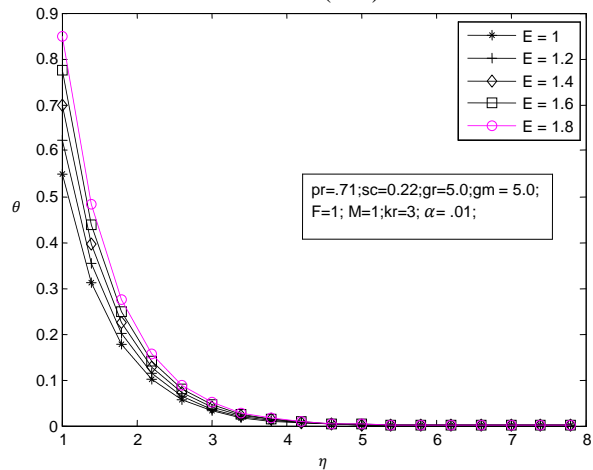


Fig.10 Temperature profile for different value of Eckert Number (E)



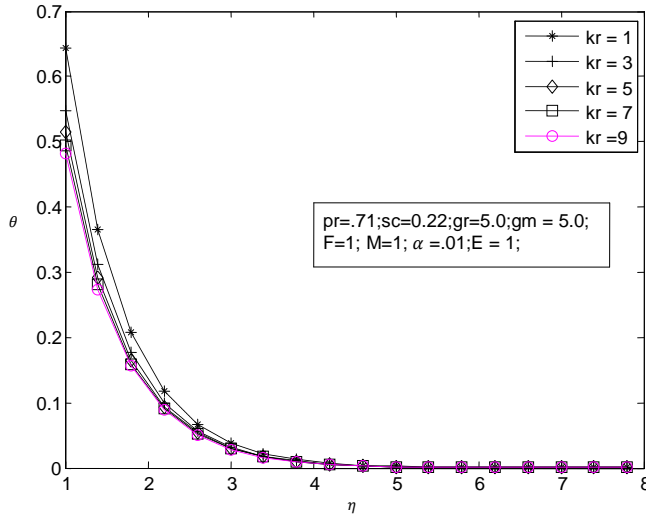


Fig.11 Temperature profile for different value of Chemical Reaction parameter ( $Kr$ )

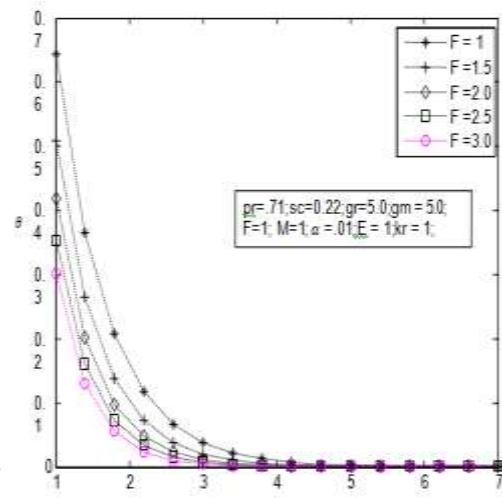


Fig.12 Temperature profile for different value of Radiation parameter ( $F$ )

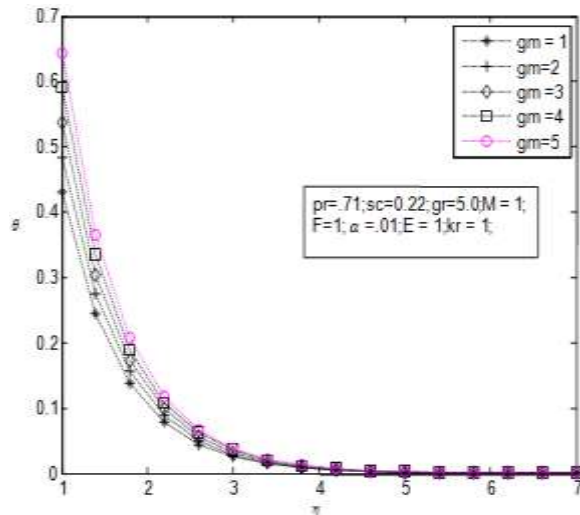


Fig.13 Temperature profile for different value of Grashof number for mass transfer ( $Gm$ )

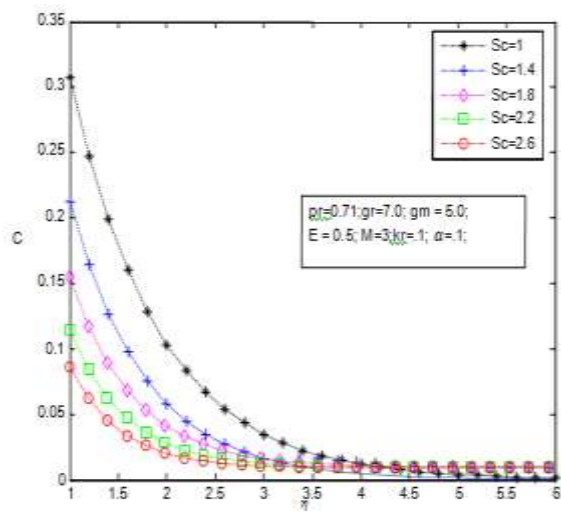


Fig.14 Concentration profile for different value of Schmidt Number ( $Sc$ )

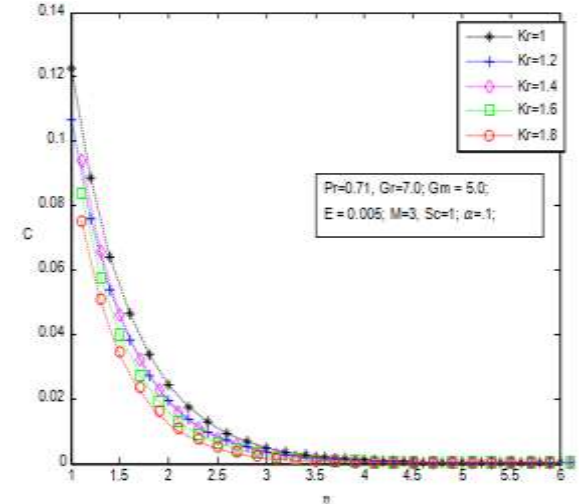


Fig.15 Concentration profile for different value of Chemical Reaction parameter ( $Kr$ )

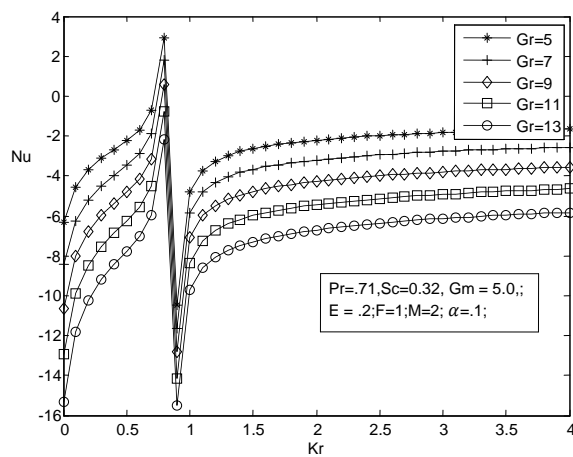


Fig.16 Nusselt Number ( $N$ ) against the thermal Grashof Number ( $Gm$ )

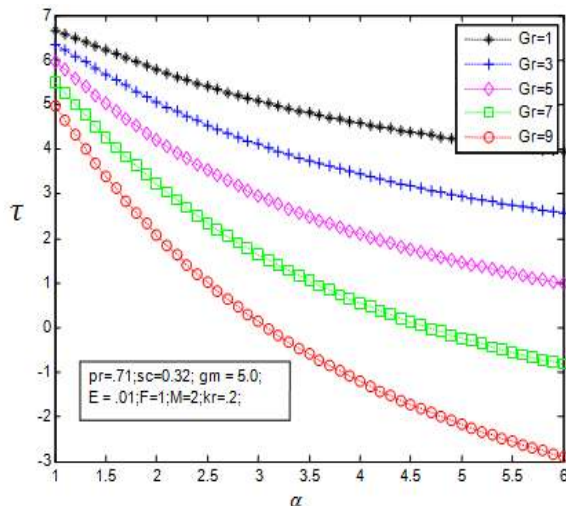


Fig.17 Skin friction against the permeability parameter different ( $\alpha$ ) with different values of Gr

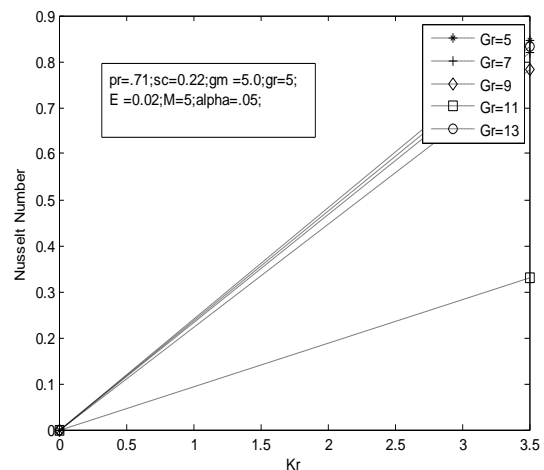


Fig.18 Nusselt Number (N) against the Kr at value of Gr

## V. COCLUSION

The problem of the influence of radiation and joule heating in presence of constant heat and mass fluxes on magneto-hydrodynamic convection flow of steady, viscous, incompressible and electrically conducting fluid past a semi infinite vertical plate embedded in a porous medium is studied. Solution of governing partial differential equations has been obtained by perturbation technique. Based on solutions, numerical computations for various values of the material parameters are carried out and following results have been observed:

1. The velocity of fluid flow increases with increase in Grashof number for mass transfer ( $G_m$ ), Grashof number for heat transfer ( $G_r$ ) Radiation parameter ( $F$ ).
2. The velocity of fluid flow decreases with increase in Schmidt number ( $Sc$ ), chemical reaction parameter ( $K_r$ ) and Prandtl Number ( $P_r$ ), Eckert Number ( $E$ ) and permeability coefficient of a porous medium ( $\alpha$ ).
3. The temperature of fluid increases with increase in Eckert Number ( $E$ ), Grashof Number ( $G_m$ ) and permeability coefficient of a porous medium ( $\alpha$ ).
4. The temperature of fluid decreases with increase in chemical reaction parameter ( $K_r$ ) and Radiation parameter ( $F$ ).
5. The concentration of fluid decreases with increase in Schmidt Number ( $Sc$ ) and chemical reaction parameter ( $K_r$ ).
6. The value Nusselt Number ( $N$ ) decreases with the increase in Thermal Grashof Number ( $G_r$ ) and increases with the increase in chemical reaction parameter ( $K_r$ )
7. The value of Skin friction decreases against thermal Grashof number ( $G_r$ ) and also decreases against permeability coefficient of a porous medium ( $\alpha$ ).

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