

Review of Applicability of Prediction Model for Running Speed on Horizontal Curve

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ABSTRACT: In Korea's road design criteria, the guideline to evaluate the safety of horizontal curve and vertical curve is quantitatively suggested, but for a complex alignment where these two alignments are combined, qualitative guideline only is provided. Thus, the measure to quantitatively evaluate the safety of the complex alignment needs to be provided as early as possible. The useful approaches to the study introduced to date include the method to use running speed profile, the method to use the sight distance and the method to use the work load and the method to evaluate the safety of road alignment using running speed profile has been more widely applied than others. Many studies on evaluating the safety of road alignment using running speed profile have been conducted domestically which however are limited to the prediction model for running speed on horizontal alignment and the study on model to predict the complex alignment combining the horizontal alignment with vertical alignment has still been far behind. This study is intended to review the method using running speed profile among the methods to evaluate the safety of complex alignment and before developing the running speed prediction model considering the effect of complex alignment, the study was conducted as part of the review of the need for developing the model which is differentiated by the type of combination of horizontal alignment and vertical alignment. As part of the process, integrated running speed prediction model using the design elements of horizontal alignment as independent variable was developed which was then classified depending on combination pattern of horizontal alignment and vertical alignment and was compared with determination coefficient of prediction model for individual running speed. As a result, prediction model for individual running speed developed depending on combination pattern of horizontal alignment and vertical alignment was able to predict the running speed more accurately than integrated running speed prediction model, which implies the need for developing the running speed prediction model including the variables that incorporate the combination characteristics of unique horizontal alignment and vertical alignment.

Keywords: road design, horizontal alignment, vertical alignment, alignment safety, running speed

I. INTRODUCTION

1.1. Background and Objective of Study

Traffic accident on road is caused by combination of three elements including driver, vehicle and road. 28% of the traffic accident was found to have been influenced directly or indirectly by road environment (geometric structure of the road, weather) which is equivalent to ₩4.6trillion of annual loss totaled ₩15.0 trillion for traffic accident.

As part of the study for evaluating the safety of geometric structure among road environment, development of running speed prediction model considering the geometric structure and evaluation of design consistency using running speed are underway recently. Such running speed prediction model is mostly based on design elements relating to horizontal alignment and the study on model to predict the complex alignment combining the horizontal alignment with vertical alignment has still been far behind.

This study thus is intended to develop the running speed prediction model which incorporates the design elements of horizontal alignment only using the speed data from the site and then review the possibility of evaluating the design consistency of the complex alignment where horizontal alignment and vertical alignment are combined.

1.2. Scope of the study and method

This study, within a spatial range of a 4-lane rural road where horizontal alignment and vertical alignment are combined and within a time range of non-peak hour when the interference among the vehicles has less effect on running speed, is aimed at investigating the driver's running speed.

A running speed prediction model that incorporates the design elements of horizontal alignment only was developed using the speed data collected from the site and furthermore, a running speed prediction model incorporating each influential factor by type classified as Table 1 and Fig. 1 depending on combination of horizontal alignment and vertical alignment. Each running speed prediction model was compared each other using determination coefficient and then the review whether a running speed prediction model incorporating the

design elements of horizontal alignment only is able to predict the running speed on vertical alignment The type A in Table 1 and Fig. 1 is the case when the horizontal curve is on a flatland (hereinafter "horizontal alignment section") and type B is the case when horizontal curve is on upward or downward alignment where a certain vertical slope is maintained (hereinafter "vertical slope section") and type C is the case when horizontal curve is on concave or convex vertical curve (hereinafter "complex alignment section")

Table 1. Classification depending on combination of horizontal alignment and vertical alignment

Type	Vertical alignment	Horizontal alignment
A	flatland	Horizontal curve
B	B1 upward slope	
	B2 downward slope	
C	C1 concave vertical curve	
	C2 convex vertical curve	

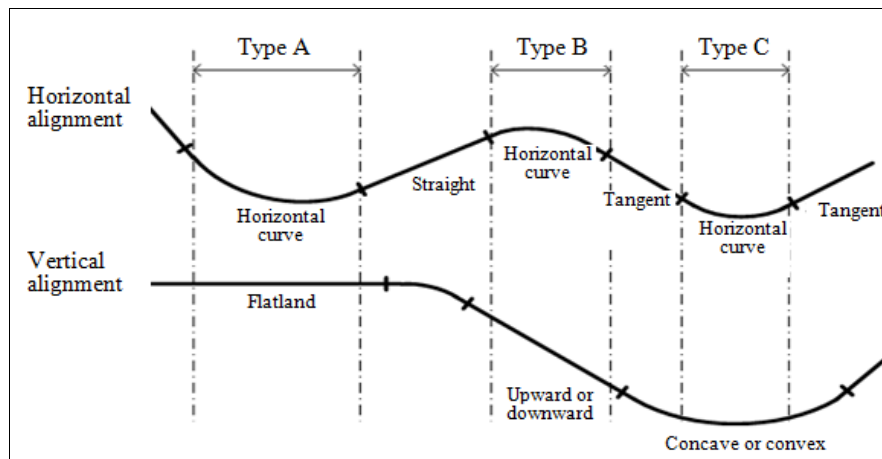


Fig. 1. Classification depending on combination of horizontal alignment and vertical alignment

II. BIBLIOGRAPHIC SEARCH

2.1 Running speed prediction model on horizontal alignment

Lamm et al (1995) proposed the model in Equation (2) below in the study on 85% of running speed and horizontal curve.

$$V_{85} = 93.87 - 3171/R, \quad R^2 = 0.787 \quad (2)$$

where, V_{85} : 85% of running speed (km/h)

R : horizontal curve radius (m)

R^2 : coefficient of determination

Kanellaidis et al (1990) proposed the relational expression between horizontal curve and running speed as follows.

$$V_{85} = 129.88 - 623.1/\sqrt{R}, \quad R^2 = 0.78 \quad (3)$$

where, V_{85} : 85% of running speed (km/h)

R : horizontal curve radius (m)

R^2 : coefficient of determination

Krammes et al (1994) proposed regression model with horizontal curve radius, angle of intersection and superelevation as independent variables.

$$V_{85} = 102.45 - 2741/R + 0.0037 - 0.10\theta, \quad R^2 = 0.82 \quad (4)$$

where, V_{85} : 85% of running speed (km/h)

R : horizontal curve radius (m)

R^2 : coefficient of determination

L : horizontal curve length (m)

θ : angle of intersection ($^\circ$)

2.2 Running speed profile model on complex alignment

Fitzpatrick et al (2000) classified it into 10 categories depending on combination of horizontal alignment and vertical alignment and proposed running speed prediction model as Table 2.

Table 2. Running speed prediction formula by alignment condition

No	Alignment conditions	Speed prediction formula
1	Horizontal curve-Vertical slope -9% ≤ G < -4%	V85=102.10- 3077.13/R
2	Horizontal curve-Vertical slope -4% ≤ G < 0%	V85=105.98 – 3709.9/R
3	Horizontal curve-Vertical slope 0% ≤ G < 4%	V85=104.82 – 3574.51/R
4	Horizontal curve-Vertical slope 4% ≤ G < 9%	V85=96.61 – 2752.19/R
5	Horizontal curve-Concave vertical curve	V85=105.32 – 3498.19/R
6	Horizontal curve-Convex vertical curve (no sight distance limit)	Min speed predicted in equation 1, 2 (downward) and 3 & 4(upward)
7	Horizontal curve-Convex vertical curve (sight distance limit)	V85=103.24 – 3576.51/R
8	Horizontal straight-Concave vertical curve	V85=assumed desired speed
9	Horizontal straight-Convex vertical curve (no sight distance limit)	V85=assumed desired speed
10	Horizontal straight-Convex vertical curve (sight distance limit)	V85=105.08 – 149.69/K

III. DATA COLLECTION AND ANALYSIS

In this study, monitoring of running speed was conducted at 66 points on national highway #5, 6, 42 and 44 as part of the effort to develop the running speed prediction model. The roads where the monitoring was conducted were high standard road where horizontal alignment and vertical alignment are distributed diversely and the data on geometric structure and driver's running speed was collected.

3.1 Selection of the points

In this study, the points which meet the principle for selection were chosen in a bid to develop the running speed prediction model that incorporates the effect by horizontal alignment and vertical alignment.

- Where no effect of intersection
- Where no effect of overspeed control system
- Where the effect by surrounding environment is minimized
- Where no school, bridge or factory that may cause abnormal situation to the driver

After surveying the candidate sites referring to the road drawing, the sites were selected finally and the distribution of the sites is as Table 3 But in type A, flatland was determined based on vertical slope ±2% or less.

Table 3. Distribution of the sites by type

Type	Vertical alignment	No	Total
A	Flatland	23	23
B	B1 Up hill	10	19
B	B2 Down hill	9	19
C	C1 Convex vertical curve	13	24
C	C2 Concave vertical curve	11	24
Total			66

3.2. Geometric structure of the road

The elements of road geometric structure were collected from road design document. The data collected were horizontal curve radius (R), horizontal curve length (CL), superelevation (e), lane width (LW), shoulder width (SW), vertical slope (G), algebraic difference of vertical slope (A), vertical curve length (Lv), distance between inflection points of horizontal curve and vertical curve (Lo) and variation rate of vertical curve (K)

Table 4 shows minimum and maximum range of road geometric structure depending on combination of horizontal and vertical alignment. Horizontal curve radius (R) is distributed over 300 ~ 3,000m while vertical

alignment (G) is -5.9 ~ 4.8%. Vertical slope difference (A) in Type C, a complex alignment is 0.7 ~ 6.3% and vertical slope variation rate (K) is 17.1 ~ 290.7.

Table 4. Geometric structure by type

Geometric element	Complex alignment type		
	Type A	Type B	Type C
R(m)	300 ~ 1,000	300 ~ 2,000	300 ~ 3,000
CL(m)	114 ~ 987	105 ~ 626	128 ~ 693
e(%)	2.0 ~ 6.5	1.5 ~ 6.9	2.0 ~ 6.0
LW(m)	3.4 ~ 3.6	3.4 ~ 3.6	3.4 ~ 3.6
SW(m)	1.3 ~ 2.0	1.0 ~ 2.5	1.5 ~ 2.3
G(%)	-1.5 ~ 1.6	-5.9 ~ 4.8	-3.8 ~ 3.6
Lv(m)	-	-	70 ~ 1,140
A(%)	-	-	0.7 ~ 6.3
L _o (m)	-	-	1 ~ 194
K(m)	-	-	17.1 ~ 290.7

3.3. Monitoring of running speed

Data on speed was collected using American nu-metrics' NC-97. The detector was 16cm wide, 14cm long and 2cm high which is not easily identified by the driver. The detector detects the vehicle passing above the magnetic field and the microcomputer in detector predicts the spot speed. The data from the detector includes vehicle speed, detection time, headway and vehicle length which are stored at the detector and then transferred to PC through RS232 port after investigation.

The data was collected at 100m ahead of the curve and in middle of the curve (hereinafter '1/2L') and additional detector was set at the point where sight distance is limited when vertical alignment in complex alignment section (type C) is in convex shape (hereinafter "convex curve") and at the peak on concave curve when vertical alignment is in concave shape (hereinafter "concave curve")

Fig. 2.shows the location of detector by type of road alignment.

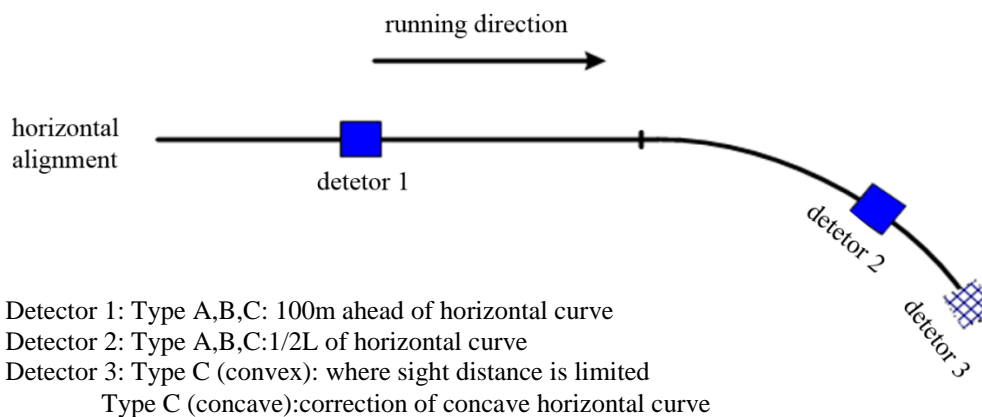


Fig.2. Location of detector by type of road alignment

In case of headway 6 seconds or less, it's excluded from the data on assumption of being influenced by other vehicles and passenger car only was included for analysis.

3.4. Development of running speed prediction model

This study is intended to determine the possibility of evaluating the design consistency in the section where horizontal alignment and vertical alignment are combined through running speed prediction model that considers horizontal alignment design element alone and thus a running speed prediction model including both horizontal alignment, vertical alignment and combined curve alignment (hereinafter called 'Integrated model') and a running speed prediction model depending on type of combination of horizontal alignment and vertical alignment (hereinafter called 'Individual model') are developed, separately.

Table 5 shows the classification by the type of combination of horizontal alignment and vertical alignment and suggests the representative type of running speed prediction model.

'Type A' is the section where horizontal curve and flatland are overlapped and as suggested by previous studies, design element of horizontal alignment (R') is the key parameter in predicting the running speed (see 1) of Table 5) 'Type B' is the horizontal curve where a certain slope is maintained and prediction model containing the design element of horizontal alignment (R') and design element of vertical slope (G') as independent variable would be important (see 2) of Table 5) 'Type C' is the case combining horizontal alignment and vertical alignment and prediction model containing design element of horizontal alignment (R') and design element relating to vertical slope (K') may be assumed (see 3) ~ 5) of Table 5).

Table 5. Running speed prediction model by type of road alignment

Type	Prediction model
A	1) $V85 = b_0 + b_1 \times R'$
B	2) $V85 = b_0 + b_1 \times R' + b_2 \times G'$
C	3) $V85 = b_0 + b_1 \times K'$ 4) $V85 = b_0 + b_1 \times R' + b_2 \times K'$ 5) $V85 = b_0 + b_1 \times (R' \times K')$
where, R'	: design element of horizontal alignment
G'	: design element of vertical slope
K'	: design element of vertical curve

Based on prediction model proposed in Table 5, integrated model with V85 as dependent variable and with design element of horizontal alignment as independent variable and individual model with design element of each type of road alignment as independent variable were developed. In this process, the lower value speed data among those from detector 2 and 3 was used.

In addition to common variables, square and square root of each variable, natural logarithms and exponential function were also reviewed for developing the prediction model. The variables considered to predict the running speed are as Table 6.

Table 6. Independent variables

Design elements of horizontal alignment (R')	
.1/R	: Curvature (m ⁻¹)
.CL	: Horizontal curve length (m)
.LW	: Lane width on horizontal curve (m)
.SW	: Shoulder width on horizontal curve (m)
.e	: Superelevation on horizontal curve (%)
Others	: Square, square root, natural logarithms and exponential function by design element of horizontal alignment
Design elements of vertical alignment (G', K')	
.G	: Vertical slope (%)
.A	: Algebraic difference of vertical slope (%)
.Lo	: Distance between inflection points of vertical curve and horizontal curve (m)
.Lv	: Vertical curve length (m)
.K	: Variation rate of vertical curve (m/%)
Others	: Square, square root, natural logarithms and exponential function by design element of vertical alignment

Independent variable of regression model was selected considering the significant design element with higher correlation with V85 and the primary regression model was developed in a way of eliminating one by one the independent variable failed to meet the elimination requirement (F=0.010) Optimal regression model was determined among the primary regression models considering the sign of independent variable, correlation between independent variables, significance of model and independent variable (F testing hypothesis, t testing hypothesis) independence between error terms (Durbin-Watson), multicollinearity (tolerance limit VIF, state index), outlier (standardized residuals).

When it comes to determination coefficient indicating the explanation power of regression equation, modified determination coefficient (adj R²) was applied to minimize the effect of increasing determination coefficient by increase in number of independent variables.

1) Integrated model

A running speed prediction model that incorporates horizontal design elements from 66 survey points was developed. Table 7. summarize the optimal integrated regression model and the regression model with 1/R and e as independent variable was found to be most persuadable. As a result of F, t test, determined regression model and individual independent variable have statistical significance and regression model determined by

residual and multicollinearity analysis was found not to be in conflict with basic assumption of regression model. A determination coefficient of optimal regression model was 0.134.

Table 7. Integrated optimal regression model

Model	Non-standardized coefficient		t	Significance probability	Colinearity statistic		R ²
	B	Standard error			Tolerance limit	VIF	
Constant	106.19	2.294	42.285	.000			.134
1/R	-7229.22	2085.702	-3.466	.001	.246	4.060	
e	3.14	1.070	2.933	.005	.246	4.060	
V85=106.19 - 7229.22×1/√R+3.14×e							
where,	V85	:	85 percentile running speed (km/h)				
	R	:	horizontal curve radius (m)				
	e	:	superelevation(%)				

2) Individual model

(1) ‘Type A’

A ‘Type A’ running speed prediction model was developed using V85 data from 23 points and horizontal alignment design element. Table 8 summarizes ‘Type A’ optimal regression model. According to analysis, regression model with 1/√R and e² as independent variable was most persuadable and determination coefficient of regression model was 0.256.

Table 8. ‘Type A’ optimal regression model 1

Model	Non-standardized coefficient		t	Significance probability	Colinearity statistic		R ²
	B	Standard error			Tolerance limit	VIF	
Constant	124.89	7.922	15.627	.000			.256
1/√R	-634.55	229.826	-2.761	.012	.420	2.378	
e ²	0.46	0.152	3.006	.007	.420	2.378	
V85=124.89 - 634.55×1/√R+0.46×e ²							
where,	V85	:	85 percentile running speed (km/h)				
	R	:	horizontal curve radius (m)				
	e	:	superelevation(%)				

Regression model with 1/R which was proposed in previous studies as independent variable is as Table 9.

Table 9. ‘Type A’ optimal regression model 2

Model	Non-standardized coefficient		t	Significance probability	Colinearity statistic		R ²
	B	Standard error			Tolerance limit	VIF	
Constant	110.76	3.697	29.957	.000			.208
1/R	-6553.45	2684.085	-2.442	.024	.443	2.258	
e	0.42	.153	2.722	.013	.443	2.258	
V85=110.76 - 6553.45×1/√R+0.42×e							
where,	V85	:	85 percentile running speed (km/h)				
	R	:	horizontal curve radius (m)				
	e	:	superelevation(%)				

As a result of F, t test, determined regression model and individual independent variable have statistical significance and regression model determined by residual and multicollinearity analysis was found not to be in conflict with basic assumption of regression model.

Individual model developed from Type A has higher determination coefficient than integrated model, indicating enhanced running speed prediction performance.

(2) ‘Type A’ + ‘Type B’

‘Type B’ running speed prediction model was planned to be developed using V85 data from 19 points and design elements with regard to horizontal alignment and vertical slope, but because of nor available of significant regression equation, a running speed prediction model was developed with total 42 points in a way of combining ‘Type A’ and ‘Type B’. Table 10 summarizes the running speed prediction model considering the integration of ‘Type A’ and ‘Type B’. Similarly with Type A running speed prediction model, regression model

with $1/\sqrt{R}$ and was independent variable was most persuadable. Determination coefficient of regression equation was 0.179, indicating lower running speed prediction performance than ‘Type A’ running speed prediction model. .

Table 10. ‘Type A’+‘TypeB’ optimal regression model

Model	Non-standardized coefficient		t	Significance probability	Colinearity statistic		R ²
	B	Standard error			Tolerance limit	VIF	
Constant	118.47	4.718	25.107	.000			.179
$1/\sqrt{R}$	-618.19	188.215	-3.285	.002	.246	4.058	
e	3.37	1.102	3.062	.004	.246	4.058	
V85=118.47 - 618.19× $1/\sqrt{R}$ +3.37×e							
where,	V85	:	85 percentile running speed (km/h)				
	R	:	horizontal curve radius (m)				
	e	:	superelevation (%)				

(3) ‘Type C’

A ‘Type C’ vertical curve running speed prediction model was developed using horizontal convex curve from 13 points and V85 data from horizontal concave curve from 11 points and vertical curve design elements

① ‘Horizontal convex curve’

Table 11 summarizes the optimal regression model of horizontal convex curve. As a result of regression analysis based on independent variables which were not excluded by removal standard, regression model with Lo and exp(e) that incorporate the relationship between horizontal curve and vertical curve as independent variables was most persuadable. Determination coefficient was 0.475 and running speed prediction performance was enhanced when comparing with determination coefficient of integrated model, 0.134.

Table 11. Optimal regression model of horizontal convex curve

Model	Non-standardized coefficient		t	Significance probability	Colinearity statistic		R ²
	B	Standard error			Tolerance limit	VIF	
Constant	112.07	2.601	43.096	.000			.475
Lo	-0.047	0.081	-2.616	.024	1.000	1.000	
exp(e)	-0.058	0.024	-2.408	.037	1.000	1.000	
V85=112.07 - 0.047×Lo-0.058×exp(e)							
Where,	V85	:	85 percentile running speed (km/h)				
	Lo	:	distance between inflection points of vertical curve and horizontal curve(m)				
	e	:	superelevation(%)				

Table 12 shows the result after removing independent variable one by one from optimal regression model. Low which is determined by correlation between horizontal alignment and vertical alignment design element was found to have larger effect on running speed prediction performance than e which is horizontal alignment design element. Such result shows that a running speed prediction model incorporating the effect by linear combination needs to be considered for the alignment where horizontal curve and vertical curve are combined.

Table 12. Regression model considering the effect of Lo or e

Model	Independent variable	Regression model	R ²
1	Lo	V85=107.22 - 0.048×Lo	.240
2	exp(e)	V85=108.97 - 0.058×exp(e)	.188
Where,	V85	:	85 percentile running speed (km/h)
	Lo	:	distance between inflection points of vertical curve and horizontal curve(m)
	e	:	superelevation %

② ‘Horizontal convex curve + horizontal concave curve’

A running speed prediction model for horizontal concave curve was planned to be developed using V85 data from 11 points and horizontal alignment and vertical curve design elements but significant regression equation was not available and thus a running speed prediction model was developed with total 24 points in a way of combining horizontal convex curve and horizontal concave curve. Table 13 summarizes the running speed prediction model that is applicable to both horizontal convex curve and horizontal concave curve. Regression model with Lo and 1/Ln(R) as independent variable was most persuadable. Determination coefficient of regression equation was 0.251, indicating a lower determination coefficient comparing to the running speed prediction model for horizontal convex curve.

Table 13. Horizontal convex curve + horizontal concave curve optimal regression model

Model	Non-standardized coefficient		t	Significance probability	Colinearity statistic		R ²
	B	Standard error			Tolerance limit	VIF	
Constant	152.37	20.707	7.358	.000			.251
1/LnR	-278.10	131.924	-2.108	.047	.994	1.006	
Lo	-0.043	0.020	-2.118	.046	.994	1.006	
$V85=110.76 - 6553.45 \times 1/\sqrt{R} + 0.42 \times e$							
where,	V85	:	85 percentile running speed (km/h)				
	R	:	horizontal curve radius (m)				
	e	:	superelevation(%)				

As a result of F, t test, determined regression model and individual independent variable have statistical significance and regression model determined by residual and multicollinearity analysis was found not to be in conflict with basic assumption of regression model.

3) Result

Optimal running speed prediction model developed from this study and determination coefficient are as Table 14.

Table 14. Optimal regress model

Model	Running speed prediction model	R ²		
1	$V85=106.19 - 7229.22 \times 1/\sqrt{R} + 3.14 \times e$.134		
2	$V85=124.89 - 634.55 \times 1/\sqrt{R} + 0.46 \times e^2$.256		
3	$V85=118.47 - 618.19 \times 1/\sqrt{R} + 3.37 \times e$.179		
4	$V85=112.07 - 0.047 \times Lo - 0.058 \times \exp(e)$.457		
5	$V85=110.76 - 6553.45 \times 1/\sqrt{R} + 0.42 \times e$.251		
Where,	Model1	:	Integrated model	
	Model2	:	Type A running speed prediction model	
	Model3	:	Model considering both Type A & B	
	Model4	:	Type C convex vertical curve running speed prediction model	
	Model5	:	Model considering both Type C convex vertical curve and concave vertical curve	

To compare and evaluate the running speed prediction models depending on type of combination of horizontal alignment and vertical alignment within the limited data, determination coefficient by model was used as the indicator and the result was obtained as follows.

- Prediction model in which the characteristics of combination of horizontal and vertical alignment are not incorporated has the lowest determination coefficient (Model 1).
- Model 3 developed using the data on horizontal alignment and vertical alignment had lower determination coefficient than model 2 developed using the data on horizontal alignment only.
- Model 5 developed using the data on both horizontal convex curve and concave curve had lower determination coefficient than model 4 using the data on horizontal convex curve.

IV. CONCLUSION

Road design consistency is the part of way to evaluate the safety of continuous road alignment and to evaluate the road safety based on this concept, accurate speed prediction model needs to be developed first. various models were developed at home and abroad to predict the running speed on horizontal alignment but the model for complex alignment combining horizontal alignment and vertical alignment has yet to be developed domestically. Given the difference in road alignment between the countries, it's more rational to develop the model considering own characteristics of each country. This study, as part of the stage before developing the

prediction model considering the effect of vertical alignment, is intended to review the feasibility of the need of the model differentiated by own combination characteristics.

To that end, integrated prediction model was developed based on overall speed data and design element of horizontal alignment and the result was compared with the prediction model developed after classifying it by type of combination of horizontal alignment and vertical alignment.

According to the result, prediction model using the design element of horizontal alignment alone was not able to accurately predict the speed on alignment which was combined with vertical alignment and thus prediction model containing the variables that incorporate both the horizontal and vertical alignment is required.

Thus, the parameters that would accurately identify the characteristics of vertical alignment are needed and the measure to effectively classify the geometric structure of the road depending on horizontal alignment and vertical alignment shall be provided.

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