Comparative Study of the Success of PI and PI-Fuzzy Controller for Induction Motor Drive using SVPWM Method

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Abstract: Asynchronous motors have a wide range of applications in the industry. Therefore, speed control of asynchronous motors is of great importance. Speed control of asynchronous motors based on vector control techniques to achieve high performance. The vector control technique, motor flux and moment variables can be controlled independently of each other. Because of the nonlinear and complex model of asynchronous motors, the speed control applications of these motors are not provided with great efficiency by classical control methods. Fuzzy logic controllers (FLC), which were successful in many areas, present great performance in speed control of a asynchronous motor. In this study, a simulation study regarding speed control of a three-phase squirrel cage asynchronous motor was carried out with a PI-Fuzzy type FLC and a conventional PI type controller. The data obtained by simulation are evaluated and the performances of the control methods are compared.

Keywords: Fuzzy Logic Control, PI type Control, Space Vector Pulse Width Modulation (SVPWM), Threephase squirrel cage asynchronous motor,

I. Introduction

Asynchronous motors are the most widely used machine in the industry due to their simple construction, low cost, reliable operation in extreme operation, low maintenance requirement and high efficiency. Scalar control method derived from steady state model and vector control methods obtained from dynamic model of motor are used in speed control of these motors [1]. In the scalar speed control method, the steady state model of the motor is used and speed control is performed by keeping the voltage / frequency ratio (V / f) as constant [2-3]. Fundamentals of achieving high performance in the speed control of asynchronous motors are based on vector control techniques. The vector control made possible to obtain a considerable dynamic performance in asynchronous motor control just as provided in free excited direct current machines.By the vector control method, the motor flux and moment variables can be controlled independent from each other. The torque, speed and acceleration of electric motors can be improved and the efficiency can be increased when these parameters are controlled with the power electronics [4-5]. The asynchronous motors require complicated control and transformation algorithms because of their nonlinear structure [6].Classical controllers exhibits low performances in the control of nonlinear systems that of their mathematical models are not well defined.Fuzzy logic, artificial neural networks or neural fuzzy controllers are more successful in controlling such systems. It is not possible to model a nonlinear system exactly [7]. The structure of the fuzzy logic controller has adaptive properties. Therefore, when FLC is used in the systems with uncertainties, variable parameters and loads, it guarantees desired responses for the system [8]. The fuzzy logic approach gives machines the ability to process special data of humanity and ability to operate by taking advantage of their experiences and expertises.By performing this ability, it uses symbolic expressions instead of numeric expressions. The basis of fuzzy logic is the controller's verbal expressions and the logical connections between them. While FLC is applied to system, mathematical modeling of the system is not required [9]. In order to make decisions, the FLC algorithm uses rules that contain information about the system. This rule based decision making mechanism, which reminds of the method used by human brain, is determined by taking the advantage of user experience. Classical logic uses a sharp concept while decision making whether an individual is a member or not a member of a set, and there is a precise boundary to determine for belonging of an individual to the set. An element belongs to a set or it does not. On the contrary, fuzzy logic considers the intermediate values [10].

In this paper, a simulation study was performed using PI-Fuzzy type fuzzy logic controller and PI type controller for speed control of an asynchronous motor with a three-phase star connected squirrel cage. Indirect field oriented control (IFOC) method was used for the drive method of asynchronous motor. This paper presents the performance of PI and PI-Fuzzy type speed control method for simulation study.

II. Mathematical Model of Three-Phase Squirrel Cageasynchronous Motor

Basically while performing the simulation study, it requires the mathematical model to determine physical behavior of a system. The most appropriate control rules for the control of system are determined with the studies on this model. The three phase variables of the motor are transferred to the dq plane in order to obtain the mathematical model of the asynchronous motor. As a result, the asynchronous motor is simulated as a direct current motor by applying the controlled field-oriented control in the d-q axis set rotating at synchronous speed. This model is arranged as a suitable format to computer analysis and simulation studies which will be used to determine control rules [4,7,11,15,17,22].



Fig. 1:a-b-c, α - β ve d-q axis set plane

For the asynchronous motor, the differential equations in the d-q axis set can be derived as the following formulas; Equivalent resistance;

$$R_{E} = R_{s} + \frac{R_{F}' L_{m}^{2}}{L_{r}^{2}}$$
(1)

Leakagefactor;

$$\sigma = 1 - \frac{L_m^2}{L_s L_r^2} \tag{2}$$

$$\frac{di_{sd}}{dt} = \frac{1}{\sigma L_s} \left[-R_E i_{sd} + \sigma L_s \omega_s i_{sq} + \frac{L_m R'_r}{L_r^2} \psi_{rd} + \omega_r \frac{L_m}{L_r'} \psi_{rq} + V_{sd} \right]$$
(3)

$$\frac{di_{sq}}{dt} = \frac{1}{\sigma L_s} \left[-R_E i_{sq} - \sigma L_s \omega_s i_{sd} - \omega_r \frac{L_m}{L_r'} \psi_{rd} + \frac{L_m R_r'}{L_r'} \psi_{rq} + V_{sq} \right]$$
(4)

$$\frac{d\psi_{rd}}{dt} = \frac{R'_{r}L_{m}}{L'_{r}}i_{sd} - \frac{R'_{r}}{L'_{r}}\psi_{rd} + \omega_{sl}\psi_{rq}$$
(5)

$$\frac{d\psi_{rq}}{dt} = \frac{R'_r L_m}{L'_r} i_{sq} - \frac{R'_r}{L'_r} \psi_{rq} - \omega_{sl} \psi_{rd}$$
(6)

$$\frac{d\omega_m}{dt} = \frac{pL_m}{JL'_r} (i_{sq}\psi_{rd} - \psi_{rq}i_{sd}) - \frac{B}{J}\omega_m$$
(7)

Sliding speed;

$$\omega_{sl} = \omega_s - \omega_r = \frac{R'_r i_{qs}}{L'_r i_{ds}}$$
(8)

Synchronous position;

$$\theta_{s} = \int \omega_{s} dt \tag{9}$$

III. Space Vector Pulse Width Modulation (SVPWM)

TheThree phase voltage with desired amplitude and phase is obtained from a simple DC voltage at inverter's three output terminals by SVPWM. Three-phase voltages previously mentioned are represented by a reference voltage space vector.

$$\vec{v}_{ref} = \vec{v}_{a} + j\vec{v}_{\beta} = \frac{2}{3} \left(v_{ao} \cdot \vec{a}^{0} + v_{bo} \cdot \vec{a}^{1} + v_{co} \cdot \vec{a}^{2} \right)$$
(10)
where $\vec{a} = e^{j\frac{2\pi}{3}}$.

The three-phase voltage source is obtained from eight possible switching positions of the three terminal inverter shown in Fig. 2 and given in Table 1.



Fig. 2: Circuit diagram of three terminal inverter and star connected motor

S 1	S2	<u>S3</u>	Vk	Va	Vb	Vc
0	0	0	\mathbf{V}_0	0	0	0
0	0	1	V_5	$-V_{dc}/3$	$-V_{dc}/3$	2V _{dc} /3
0	1	0	V ₃	$-V_{dc}/3$	$2V_{dc}/3$	-V _{dc} /3
0	1	1	V_4	-2V _{dc} /3	$V_{dc}/3$	V _{dc} /3
1	0	0	V ₁	$2V_{dc}/3$	$-V_{dc}/3$	-V _{dc} /3
1	0	1	V ₆	$V_{dc}/3$	-2V _{dc} /3	V _{dc} /3
1	1	0	V_2	$V_{dc}/3$	$V_{dc}/3$	-2V _{dc} /3
1	1	1	V ₇	0	0	0

Table 1: Eight switching positions and voltage vectors

The six nonzero active state space vectors can be stated as in Equation 11.

$$\vec{v}_{k} = \frac{2}{3} v_{dc} e^{j(k-1)\frac{\pi}{3}} \qquad k=1,2,3,4,5,6$$
(11)

Here, the two adjacent active vectors can be expressed as the following with equation 12 and 13.

$$\vec{V}_{k} = \frac{2}{3} V_{dc} \left[\cos(k-1)\frac{\pi}{3} + j\sin(k-1)\frac{\pi}{3} \right]$$
(12)

$$\vec{v}_{k+1} = \frac{2}{3} v_{dc} \left[\cos \frac{k\pi}{3} + j \sin \frac{k\pi}{3} \right]$$
(13)

When the voltage vector V_{ref} is examined on the α - β axis, six space vectors will form when the output voltages are checked for period T.These vectors are placed at 60° degree intervals on the axis set.This case is shown in Fig. 3.



Fig. 3:Demonstration of space vectors on the α - β axis

 V_{ref} is defined as the average space vector in each switching period Ts. The V_{ref} voltage vector can be expressed as a combination of vectors 0 and 7 in each of the six regions and a weighted average of the two adjacent active space vectors. When V_{ref} is assumed in region k, in this case adjacent vectors will be V_k and V_{k+1} . While switching from a position to another, switching position of only a terminal in inverter will be changed. This operation also provides the best harmonic performance. The V_{ref} voltage vector is stated as in equation 14. Where Ts is sampling time.]. In case Ts is assumed to be as small as possible, then V_{ref} is assumed to be approximately constant [18-20, 23].

$$\begin{array}{c} \overline{V_{ref}} & \frac{T_s}{2} = \overline{V_k T_k} + \overline{V_{k+1} T_{k+1}} \\ \left[V_{\alpha} \\ V_{\beta} \\ \end{array} \right] \frac{T_s}{2} = \frac{2}{3} V_{dc} \left[\begin{array}{c} \cos(k-1) \frac{\pi}{3} & \cos\frac{k\pi}{3} \\ \sin(k-1) \frac{\pi}{3} & \sin\frac{k\pi}{3} \\ \sin(k-1) \frac{\pi}{3} & \sin\frac{k\pi}{3} \\ \end{array} \right] \left[T_k \\ T_{k+1} \\ \end{array} \right] \\ = \frac{\sqrt{3}}{2} \frac{T_s}{V_{dc}} \left[\begin{array}{c} \sin\frac{k\pi}{3} & -\cos\frac{k\pi}{3} \\ -\sin(k-1) \frac{\pi}{3} & \cos(k-1) \frac{\pi}{3} \\ -\sin(k-1) \frac{\pi}{3} & \cos(k-1) \frac{\pi}{3} \\ \end{array} \right] \left[V_{\alpha} \\ V_{\beta} \\ \end{array} \right] \tag{15}$$

Where T_k and T_{k+1} are the times for applying the voltages $V_k veV_{k+1}$. T_0 is the time for applying the zero voltage vector $(V_0 \text{ or } V_7)$ [10].

$$T_{k} = \frac{\sqrt{3}}{2} \frac{T_{s}}{V_{dc}} (V_{\alpha} \sin \frac{k\pi}{3} - V_{\beta} \cos \frac{k\pi}{3})$$
(17)

$$T_{k+1} = \frac{\sqrt{3}}{2} \frac{T_s}{V_{dc}} \left(-V_{\alpha} \sin(k-1) \frac{\pi}{3} + V_{\beta} \cos(k-1) \frac{\pi}{3} \right)$$
(18)

$$\frac{T_s}{2} = T_0 + T_k + T_{k+1} \Rightarrow T_0 = \frac{T_s}{2} - T_k + T_{k+1}$$
(19)

The switching system will be different for each region. The switching design for region I is shown in figure 4.



Fig. 4:SVPWM switching for Region I

IV. **Fuzzy logic control**

A FLC block diagram is shown in figure 5.FLC consists of four basic components which are fuzzification, fuzzy inference, defuzzification and knowledge base.

(16)



Fig. 5: Block diagram of fuzzy logic controller

Fuzzification is the process that firstly a crisp set of input data taken from a system are converted to a fuzzy set using fuzzy linguistic variables, fuzzy linguistic terms and membership functions. Fuzzy inference is made based on a set of rules. This unit provides fuzzy output set by applying the fuzzy input set to the rules of rule base. The most widely used method in fuzzy inference methods and the method used in this study is the Mamdani method.Defuzzification, the resulting fuzzy output is converted to a crisp output using the membership functions. Consequently, this process provides the real values which will be used in application. Knowledge base consists of a data table that hosts information about the system. Connections between inputs and outputs are provided using rule-based rules. While a rule base is developed for a system, input values that can affect the output of system are supposed to be well determined. Fuzzy control rules are usually constituted by expert knowledge [11-14, 16, 21].

IV.I. PI-Fuzzy Type Control

In classical PI type controller, K_p is the proportional gain constant, and K_i is the integral gain constant.

$$u(t) = Kp.e(t) + Ki.\int e(t)dt$$

(20)

The PI-Fuzzy type control system is a two-input single-output fuzzy system referenced to the classical PI control system. Where K_i is the gain factor used with error, and K_p is the gain factor used with error variance. The block diagram of PI-Fuzzy type controller is shown in fig. 6 [24].



Fig. 6: PI-Fuzzy type Controller

V. Simulation Results

MATLAB is used in simulation studies of speed control of asynchronous motor.Parameters of the asynchronous motor are listed as the following:

P=3 kW	n=1430 rpm	p=2	L _m =0,1878 H
U=380 V	$R_s=1,45\Omega$	$L_{s} = 0,2 H$	J=0,03 kg.m ²
I=6,7 A	$R_r = 1,93 \Omega$	M=10 Nm	B=0,03Nm.san/rad

Resulting values from motor output are compared to reference values and flux information, and error values are obtained. By using these values, required transformations and calculations have been performed for modulation. The optimal switching vector detection of the inverter is performed considering the sector in which the reference voltage vector is located. The motor is drived by applying The SVPWM signals obtained by calculating the durations of these vector to the inverter. In study, sampling time Ts= 0.2ms. The block diagram of the study is seen in fig. 7. In this study, two inputs are selected for each PI-Fuzzy type controller. Where error (*e*) and error change (*de*).k is the iteration number, and the error and error change are expressed as the following:



$$de_q(k) = e_q(k) \cdot e_q(k-1) \tag{23}$$

$$P_d(k) = i_{sdref}(k) \cdot i_{sd}(k) \tag{24}$$

 $de_d(k) = e_d(k) - e_d(k-1)$ (25)



Fig. 7: Design of IFOC based FLC architecture

In the fuzzification step, input and output information received from the system are converted to symbolic expressions which are linguistic variables. Inputs and outputs in the specified range are represented with seven different symbolic expressions. These are NL (Negative Large), NM (Negative Medium), NS (Negative Small), Z (Zero), PS (Positive Small), PM (Positive Medium), PL (Positive Large), respectively. Selection of the membership functions for each input and output is optional among triangular, trapezoidal, sinusoidal, cauchy, bell, sigmoid, gaussian. Five triangular and two trapezoidal membership functions are used for input and output in the system. These membership functions are shown in fig. 8 [14, 17, 25].



Fig. 8: Fuzzy output membership functions

In the fuzzy inference unit, the relation of the inputs with output is provided by the rules constituting the rule base. There are 49 rules in the study of Rule Editor of Matlab / Fuzzy Logic Toolbox / FIS. The rule table is shown in Table 2.

Table 2: Fuzzy rule table							
e ∆e	NB	NM	NS	Z	PS	PM	PB
NB	NB	NB	NB	NB	NM	NS	Ζ
NM	NB	NB	NM	NM	NS	Ζ	PS
NS	NB	NM	NS	NS	Ζ	PS	PM
Ζ	NB	NM	NS	Ζ	PS	PM	PB
PS	NM	NS	Ζ	PS	PS	PM	PB
PM	NS	Ζ	PS	PM	PM	PB	PB
PB	Ζ	PS	PM	PB	PB	PB	PB

. .

In defuzzification unit, the membership weights of error and change of error are obtained for each rule, afterwards, minimum terms of membership weight are determined for each region and output membership values are determined accordingly. The values obtained in the output of the fuzzification unit are VsdveVsq voltages. The supply voltage of the inverter is 550V DC and the switching frequency is 5 kHz. For simulation study of asynchronous motor, the reference speed is given as 110 and 120 rad / s one by one. The motor is loaded with 10 Nm at the 1st second. The resulting simulation of PI-Fuzzy type FLC is shown in fig. 9, 10, 11, and 12.



Simulation study of asynchronous motor, the reference speed is given as 110 and 120 rad / s one by one. The motor is loaded with 10 Nm at the 1st second. The resulting simulation of conventional PI type control is shown in fig. 13, 14, 15, and 16.



When the speed versus time graph in fig. 12 and fig. 16 are reviewed, it is reveal that nominal speed has reached the reference speed faster in PI-Fuzzy control technique than PI control. Also, this situation is understood from the table 3. The performance parameters of the controllers are the rise time t_r , settling time t_y and overshoot %M, respectively. The parameter values are given in Table 3.

Table 5. Initia	performance values of control			
Control	$t_r(s)$	t _y (s)	%M	
PI-Fuzzy	0.08	0.18	1	
PI	0.15	0.21	0	

Table 3: Initial performance values of control

VI. Conclusion

Because of the fact that asynchronous motors have a wide range of applications in the industry, it requires to control these motors efficiently. In this study, speed control of a star connected three-phase squirrel cage asynchronous motor is performed with PI-Fuzzy type controller and PI type controller using IFOC method. Basic control signals of the control, there has been created control blocks in the form of stator voltages in the d-c coordinate system. When we examine the obtained graphs, overshoot in PI-Fuzzy type control at the regions that reference speed change is higher than the overshoot occurred in PI control. Overshoot in PI-Fuzzy type control has smaller rise time and settling time when compared to PI type control. As a result, the performance of control processes for both controllers is clearly seen with the simulation results. By investigating the points of motor loading and rapid changing in the given reference speed orbit, the deviations occurred in that process has been removed in a short time. In conclusion, by considering all operating conditions, the PI-Fuzzy logic technique had clearly revealed better performance than PI controller in order for faster minimization of the error.

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